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Characteristic Velocity for Conduction and Mean Free Path Characteristic Velocity:

The characteristic velocity is the average velocity of those electrons that contribute to the conductivity: $d\vec{\mu} = (25(r))$

$$\left\langle \mathbf{v}^{2} \right\rangle = \frac{\int \frac{\mathbf{d}^{d} \mathbf{k}}{(2\pi)^{d}} \left(-\frac{\partial f(\mathbf{E})}{\partial \mathbf{E}} \right) \mathbf{v}(\mathbf{\bar{k}}) \cdot \mathbf{v}(\mathbf{\bar{k}})}{\int \frac{\mathbf{d}^{d} \mathbf{\bar{k}}}{(2\pi)^{d}} \left(-\frac{\partial f(\mathbf{E})}{\partial \mathbf{E}} \right)}$$

For metals and heavily doped semiconductors at low temperatures: $\sqrt{\langle v^2 \rangle} \approx v_F$

For low doped semiconductors at high temperatures: $\sqrt{\langle \mathbf{v}^2 \rangle} \approx \sqrt{\frac{d KT}{m_e}}$

Mean Free Path:

The mean free path ℓ is defined as the average distance an electron travels before it scatters. It is given by:

$$\ell = \sqrt{\langle \mathbf{v}^2 \rangle} \tau$$

where au is the scattering time.

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The length scales involved in the smallest transistors and nanoscale devices, such as carbon nanotubes and molecular conductors, can be small enough so that the electrons do not scatter during the time it takes to travel through the device







Electron Currents

At the left contact, the current due to electrons moving in the right direction is:

$$I_{L \to R} = (-e)2 \times \int_{0}^{\infty} \frac{dk_z}{2\pi} v_c(k_z) f(E_c(k_z) - E_{fL})$$

At the right contact, the current due to electrons moving in the left direction is:

$$I_{R \rightarrow L} = (-e)2 \times \int_{-\infty}^{0} \frac{dk_z}{2\pi} v_c(k_z) f(E_c(k_z) - E_{fR})$$

The direction of electron flow (not the direction of current, which is opposite)

$$F_{fL} \downarrow eV$$

$$E_{fL} \downarrow eV$$

$$E_{c} + E_{1}$$

$$E_{c} + E_{1}$$

$$E_{c} + E_{1}$$

$$E_{c} + E_{1}$$

$$K_{z}$$





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Conductance as Transmission: Landauer's Formula

$$I = (-e)2 \times \int_{0}^{\infty} \frac{dk_{z}}{2\pi} v_{c}(k_{z}) T_{c} f(E_{c}(k_{z}) - E_{fL}) + (-e)2 \times \int_{-\infty}^{0} \frac{dk_{z}}{2\pi} v_{c}(k_{z}) f(E_{c}(k_{z}) - E_{fR})$$

$$+ (-e)2 \times \int_{0}^{\infty} \frac{dk_{z}}{2\pi} v_{c}(k_{z}) R_{c} f(E_{c}(k_{z}) - E_{fR})$$

$$= e 2 \times \int_{0}^{\infty} \frac{dk_{z}}{2\pi} v_{c}(k_{z}) T_{c} [f(E_{c}(k_{z}) - E_{fR}) - f(E_{c}(k_{z}) - E_{fL})]$$

$$= 2 \times \frac{e T_{c}}{2\pi \hbar} \int_{E_{c} + E_{1}}^{\infty} dE [f(E - E_{fR}) - f(E - E_{fL})]$$

$$= \left(\frac{e^{2}}{\pi \hbar} T_{c}\right) V$$

$$\Rightarrow G = \frac{e^{2}}{\pi \hbar} T_{c} < G_{Q}$$

$$E \int_{E_{c}} \frac{e^{2}}{\pi \hbar} T_{c}$$

$$= e 2 \times \frac{e T_{c}}{\pi \hbar} \int_{E_{c}}^{\infty} \frac{e^{2}}{\pi \hbar} \int_{E_{c}}^{\infty} \frac{e^{$$

Conductance as Transmission: Higher Dimensions

$$F_{f_{L}} \underbrace{eV} \underbrace{f_{f_{L}}}_{d-dimensional material}} \underbrace{F_{f_{L}}}_{d-dimensional material}} \underbrace{f_{L}}_{f_{L}} \underbrace{f_{L}}_{y} \underbrace{f_{L}}_{y}$$

