





Generation and Recombination in Thermal Equilibrium

• From the first lecture, in thermal equilibrium:

The recombination rate = $R_o = k n_o p_o$ equals the generation rate = G_o

i.e.
$$G_o = R_o$$

• Then in thermal equilibrium:

$$\frac{\partial n_o(t)}{\partial t} = G_o - R_o = 0$$
$$\frac{\partial p_o(t)}{\partial t} = G_o - R_o = 0$$





Generation and Recombination Out of Thermal Equilibrium • We can use the equations: $\frac{\partial n(t)}{\partial t} = G - R \qquad \frac{\partial p(t)}{\partial t} = G - R \qquad n = n_0 + n'(t) \\ p = p_0 + n'(t)$ • Generation rate: $G = G_0 + G_L$ • Recombination rate: $R = k n p \\ = k (n_0 + n') (p_0 + p') \\ \approx k (n_0 + n') p_0 \\ = k n_0 p_0 + k n' p_0 \\ = R_0 + \frac{n'}{\tau_n}$ Assumptions: $n', p' << p_0$ $\frac{1}{\tau_n} = k p_0 \end{cases}$ $\frac{\tau_n \text{ is the lifetime of the minority carriers (i.e. electrons)} \\ \text{minority carriers (i.e. electrons)}$ • The equation for excess minority carriers (i.e. electrons) becomes: $\frac{\partial n(t)}{\partial t} = G - R \longrightarrow \frac{\partial n'(t)}{\partial t} = G_0 + G_L - R_0 - \frac{n'(t)}{\tau_n} \longrightarrow \frac{\partial n'(t)}{\partial t} = G_L - \frac{n'(t)}{\tau_n}$

Generation and Recombination Out of Thermal Equilibrium $\frac{\partial n'(t)}{\partial t} = G_L - \frac{n'(t)}{\tau_n}$ • Solution with the boundary condition, n'(t = 0) = 0, is: $n'(t) = G_L \tau_n \left(1 - e^{-\frac{t}{\tau_n}}\right)$ • Excess hole density is, of course : p'(t) = n'(t)• As $t \to \infty$ the excess electron and hole densities reach a steady state value $n'(t \to \infty) = G_L \tau_n$ and $n(t \to \infty) = n_0 + G_L \tau_n$ $p'(t \to \infty) = G_L \tau_n$ and $p(t \to \infty) = p_0 + G_L \tau_n$



Generation and Recombination Out of Thermal Equilibrium • We can use the equations: $\frac{\partial n(t)}{\partial t} = G - R \qquad \frac{\partial p(t)}{\partial t} = G - R \qquad \begin{cases} n = n_0 + n'(t) \\ p = p_0 + p'(t) \end{cases}$ • Generation rate: $G = G_0$ • Recombination rate: $R = k n p \\ = k (n_0 + n') (p_0 + p') \\ \approx k (n_0 + n') p_0 \\ = k n_0 p_0 + k n' p_0 \\ = R_0 + \frac{n'}{\tau_n} \end{cases}$ Assumptions: n', p' << p_0 The excess recombination rate is proportional to the excess MINORITY carrier density • The equation for excess minority carriers (i.e. electrons) becomes: $\frac{\partial n(t)}{\partial t} = G - R \longrightarrow \qquad \frac{\partial n'(t)}{\partial t} = G_0 - R_0 - \frac{n'(t)}{\tau_n} \longrightarrow \frac{\partial n'(t)}{\partial t} = G_L - \frac{n'(t)}{\tau_n}$







Electron and Hole Current Continuity Equations

• You have already seen the equations:

$$\frac{\partial n(x,t)}{\partial t} = G - R$$
$$\frac{\partial p(x,t)}{\partial t} = G - R$$

These equations tell how the electron and hole densities change in time as a result of recombination and generation processes.

 \bullet Carrier densities can also change in time if the current densities change in space $\ref{eq:space}$













